

科目：人工智慧(A)

日期：101年1月16日 第1頁共1頁

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\* 請將答案依題號順序寫入答案卷

答題時字跡需工整，否則不予計分。Write your answers legibly; otherwise you will get zero score.

1. (15 pts) Suppose that a learning algorithm is trying to find a consistent hypothesis. There are  $n$  Boolean attributes plus one Boolean class, and examples are drawn uniformly from all possible examples. Calculate the number of examples required when the probability of finding a contradicting hypothesis with error rate 0.1 reaches 0.5. Note. Just show your expressions and procedures.
2. (12 pts) Suppose that an attribute splits the set of examples  $E$  into subset  $E_i$ , and that each subset has  $p_i$  positive examples and  $n_i$  negative examples. Show that unless the ratio  $p_i / (p_i + n_i)$  is the same for all  $i$ , the attribute has strictly positive information gain.
3. (8 pts) Define maximum-likelihood hypothesis and maximum a posteriori hypothesis. Describe their relationship briefly.
4. (15 pts) In some situation that for any unseen example, the hypothesis space contains as many consistent hypotheses predicting a positive outcome as predicting a negative outcome, how do you relate this dilemma with inductive bias and how do you get away with it?

◎ 請用深黑色鋼筆或原子筆出題

命題老師簽名：

科目：人工智慧(B)

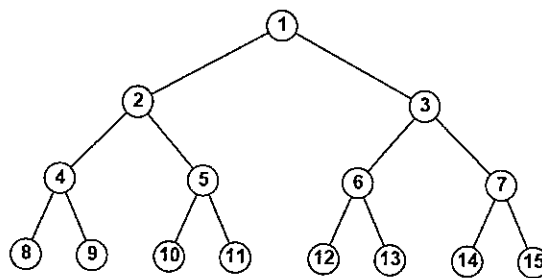
日期：101年1月16日 第1頁共2頁

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1. Given a Tree  $G(V, E)$  as Figure 1. Let the depth for node  $v \in V$  be  $d(v)$ , and edge cost for edge  $e \in E$  be  $g(e)$ .

Figure 1:  $G(V, E)$ 

- (a) List the order in which nodes will be visited from node 1 to 11 using iterative deepening search. (5 points)
- (b) What the evaluation function  $f(v)$  can be for implementing DFS in the Figure 1 so that it can show DFS is a special case of Best-first search in which a node  $v$  is selected for expansion based on  $f(v)$ . (5 points).
2. Indicate which statements are false and correct them if false (10 points):
- (a) Simplified memory bounded A\* algorithm is complete if its all memory  $M \leq \text{depth } d$ .
- (b) In most cases,  $b^d$  is good estimate of the storage requirement for iterative deepening A\* ( $b$  is branch and  $d$  is depth)
- (c) The total number of nodes at depth  $d$  is  $bd$  for uniform search space of uniform branching factor  $b$ .
- (d) For reasonable  $b$  (say,  $b$  is less than 1000), the total number of nodes examined for alpha-beta pruning will be roughly  $O(b^d)$
- (e) The search space of A\* grows exponentially unless the error in the heuristic function grows faster than the logarithm of the actual path cost.

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3. Consider the following database of sentences in FOL:

(1)  $\forall x \quad A(x) \wedge \neg B(x) \Rightarrow \neg F(x)$

(2)  $\forall x \quad B(x) \wedge \neg C(x) \Rightarrow F(x)$

(3)  $\forall x \quad C(x) \wedge \neg D(x) \Rightarrow \neg F(x)$

(4)  $\forall x \quad D(x) \Rightarrow F(x)$

(a) How the database sentences should be modified if new sentence  $E(x) \Rightarrow \neg F(x)$  is added into. (5 points)(b) Rewrite the original database so that  $E(x) \Rightarrow \neg F(x)$  can be easily added without modifying the original database. (10 points)4. (1) Represent the following in FOL, using  $\text{times}(X,Y,Z)$  to represent the fact that  $X*Y=Z$ :  
Axioms (5 points):a. If  $X$  is prime and  $X$  divides  $Y*Z$ , then either  $X$  divides  $Y$  or  $X$  divides  $Z$ .b.  $X*X=\text{square}(X)$ 

c. Times is commutative.

d. If  $X*Y=Z$ , then  $X$  divides  $Z$ .

Theorem:

e. If  $A$  is a prime number and  $A*\text{square}(C)=\text{square}(B)$ , then  $A$  divides  $B$ .

(2.) Find the clausal forms for problem (a-d), and the clausal form for the negation of the theorem (e) (5 points)

(3.) Draw a proof tree which uses these clauses to prove (e). (5 points)