

國立交通大學試題紙

九十八學年度第一次
博士班資格考

科目：生物統計

日期：99年1月29日 第1頁共2頁

請“✓”明 ✓不可看書 可看書

* 請將答案依題號順序寫入答案卷

答題時字跡需工整，否則不予計分。Write your answers legibly; otherwise you will get zero score.

1. (60 points) Suppose that a fair coin is to be tossed n times independently. This means that the probability of getting a head is $1/2$. Let $X_i = 1$ if a head is obtained in the i th toss; and $X_i = 0$ if a tail is obtained. Let $\bar{X} = \sum_{i=1}^n X_i / n$ and $\Pr(X_i = 1) = p$.

- (10 points) What is the exact distribution of $\sum_{i=1}^n X_i$? (State its name and the parameters)
- (5 points) Derive the formula of $\text{Var}(\bar{X})$.
- (10 points) Write down the formula, based on (a), for computing $\Pr(0.4 \leq \bar{X} \leq 0.6)$.

The objective is to determine the smallest sample size n so that $\Pr(0.4 \leq \bar{X} \leq 0.6) \geq 0.8$. However the answer is not easy to obtain using the exact formula in (b).

- (15 points) Use the normal approximation to find the smallest sample size such that $\Pr(0.4 \leq \bar{X} \leq 0.6) \geq 0.8$.
(The normal table is attached.)

An experiment was conducted to test whether the coin is fair which means the probability of getting a head is $1/2$. The coin was tossed $n = 30$ times and there were total 18 heads.

- (10 points) What is the estimated value of p ?
- (10 points) Construct an approximate 95% confidence interval for p based the normal approximation result.

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2. (40 points) In a study of the risk factors for invasive cervical cancer, the following data were collected relating smoking status to the presence or absence of the cancer.

	smoker	Non-smoker	Total
Cancer	108 ()	117 ()	225
No cancer	163 ()	268 ()	431
Total	271	385	656

- a. (20 points) Compute the relative risk or the odds ratio. Use the result to explain whether there is any association between smoking status and the presence of cervical cancer.
- b. (20 points) Use the Chi-squares test to test the null hypothesis that *there is no association between smoking status and the presence of cervical cancer* at the 0.05 level of significance. The Chi-squares test table is attached.

Note: First fill in the expected number, under the null hypothesis, in the parenthesis of each cell.

Table entry for p is the critical value x^* with probability p lying to its right.

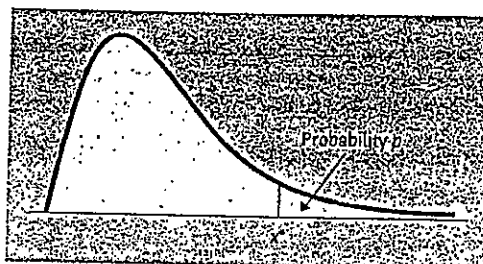


TABLE E Chi-square distribution critical values

df	p											
	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.32	1.64	2.07	2.71	3.84	5.02	5.41	6.63	7.88	9.14	10.83	12.12
2	2.77	3.22	3.79	4.61	5.99	7.38	7.82	9.21	10.60	11.98	13.82	15.20
3	4.11	4.64	5.32	6.25	7.81	9.35	9.84	11.34	12.84	14.32	16.27	17.73
4	5.39	5.99	6.74	7.78	9.49	11.14	11.67	13.28	14.86	16.42	18.47	20.00
5	6.63	7.29	8.12	9.24	11.07	12.83	13.39	15.09	16.75	18.39	20.51	22.11
6	7.84	8.56	9.45	10.64	12.59	14.45	15.03	16.81	18.55	20.25	22.46	24.10
7	9.04	9.80	10.75	12.02	14.07	16.01	16.62	18.48	20.28	22.04	24.32	26.02
8	10.22	11.03	12.03	13.36	15.51	17.53	18.17	20.09	21.95	23.77	26.12	27.87
9	11.39	12.24	13.29	14.68	16.92	19.02	19.68	21.67	23.59	25.46	27.88	29.67
10	12.55	13.44	14.53	15.99	18.31	20.48	21.16	23.21	25.19	27.11	29.59	31.42
11	13.70	14.63	15.77	17.28	19.68	21.92	22.62	24.72	26.76	28.73	31.26	33.14
12	14.85	15.81	16.99	18.55	21.03	23.34	24.05	26.22	28.30	30.32	32.91	34.82
13	15.98	16.98	18.20	19.81	22.36	24.74	25.47	27.69	29.82	31.88	34.53	36.48
14	17.12	18.15	19.41	21.06	23.68	26.12	26.87	29.14	31.32	33.43	36.12	38.11
15	18.25	19.31	20.60	22.31	25.00	27.49	28.26	30.58	32.80	34.95	37.70	39.72
16	19.37	20.47	21.79	23.54	26.30	28.85	29.63	32.00	34.27	36.46	39.25	41.31
17	20.49	21.61	22.98	24.77	27.59	30.19	31.00	33.41	35.72	37.95	40.79	42.88
18	21.60	22.76	24.16	25.99	28.87	31.53	32.35	34.81	37.16	39.42	42.31	44.43
19	22.72	23.90	25.33	27.20	30.14	32.85	33.69	36.19	38.58	40.88	43.82	45.97
20	23.83	25.04	26.50	28.41	31.41	34.17	35.02	37.57	40.00	42.34	45.31	47.50
21	24.93	26.17	27.66	29.62	32.67	35.48	36.34	38.93	41.40	43.78	46.80	49.01
22	26.04	27.30	28.82	30.81	33.92	36.78	37.66	40.29	42.80	45.20	48.27	50.51
23	27.14	28.43	29.98	32.01	35.17	38.08	38.97	41.64	44.18	46.62	49.73	52.00
24	28.24	29.55	31.13	33.20	36.42	39.36	40.27	42.98	45.56	48.03	51.18	53.48
25	29.34	30.68	32.28	34.38	37.65	40.65	41.57	44.31	46.93	49.44	52.62	54.95
26	30.43	31.79	33.43	35.56	38.89	41.92	42.86	45.64	48.29	50.83	54.05	56.41
27	31.53	32.91	34.57	36.74	40.11	43.19	44.14	46.96	49.64	52.22	55.48	57.86
28	32.62	34.03	35.71	37.92	41.34	44.46	45.42	48.28	50.99	53.59	56.89	59.30
29	33.71	35.14	36.85	39.09	42.56	45.72	46.69	49.59	52.34	54.97	58.30	60.73
30	34.80	36.25	37.99	40.26	43.77	46.98	47.96	50.89	53.67	56.33	59.70	62.16
40	45.62	47.27	49.24	51.81	55.76	59.34	60.44	63.69	66.77	69.70	73.40	76.09
50	56.33	58.16	60.35	63.17	67.50	71.42	72.61	76.15	79.49	82.66	86.66	89.56
60	66.98	68.97	71.34	74.40	79.08	83.30	84.58	88.38	91.95	95.34	99.61	102.7
80	88.13	90.41	93.11	96.58	101.9	106.6	108.1	112.3	116.3	120.1	124.8	128.3
100	109.1	111.7	114.7	118.5	124.3	129.6	131.1	135.8	140.2	144.3	149.4	153.2